Popper and the Quantum Theory

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Introduction

Popper wrote extensively on the quantum theory. In Logik der Forschung (LSD) he devoted a whole chapter to the topic, while the whole of Volume 3 of the Postscript to the Logic of Scientific Discovery is devoted to the quantum theory. This volume entitled Quantum Theory and the Schism in Physics (QTSP) incorporates a famous earlier essay, Quantum Mechanics Without "the Observer" (QM). In addition Popper's development of the propensity interpretation of probability was much influenced by his views on the role of probability in quantum theory, and he also wrote an important critique of the 1936 paper of Birkhoff and von Neumann on non-distributive quantum logic (BvNI&M). [In this paper I will look at some of Popper's arguments in a sentirely critical spirit. But he would have applauded this. My great regret is that he cannot respond to this paper with criticisms of my arguments!

1. Thought Experiments

In 1934 Popper published a short note in Die Naturwissenschaften entitled 'Zur Kritik der Ungenauigkeitsrelationen' (KU). This was actually Popper's scientific debut. It contained what Popper later described as 'a gross mistake for which I have been deeply sorry and ashamed ever since' (QTSP, 15). Appendix *XII to the 1959 translation of LSD reproduces a letter from Einstein written in 1935 criticizing Popper's proposed thought experiment. Although he tells us in his autobiography (UQ, 92) that he had defended his experiment against von Weizsäcker and Heisenberg, he immediately conceived with Einstein's criticism. Einstein was Popper's great scientific hero, and the example of the successful novel prediction of general relativity was the paradigm example of Popperian corroboration, although as we shall see later, Popper was in fundamental disagreement with Einstein on the epistemic status of determinism in quantum mechanics. Although Popper's understanding of the physics involved in his thought experiment was defective at best, as we shall explain shortly, nevertheless there is a definite sense in which Popper had anticipated an important experiment in the famous Einstein–Podolsky–Rosen (EPR) paper of 1935. One can even speculate that Einstein was influenced by Popper here[2] (For historical details see Jammer, 178). Popper himself remarked in a letter to Max Jammer in 1967, with a humility that was more characteristic of Popper in matters of physics than

Figure 1. Incident on p. 3.

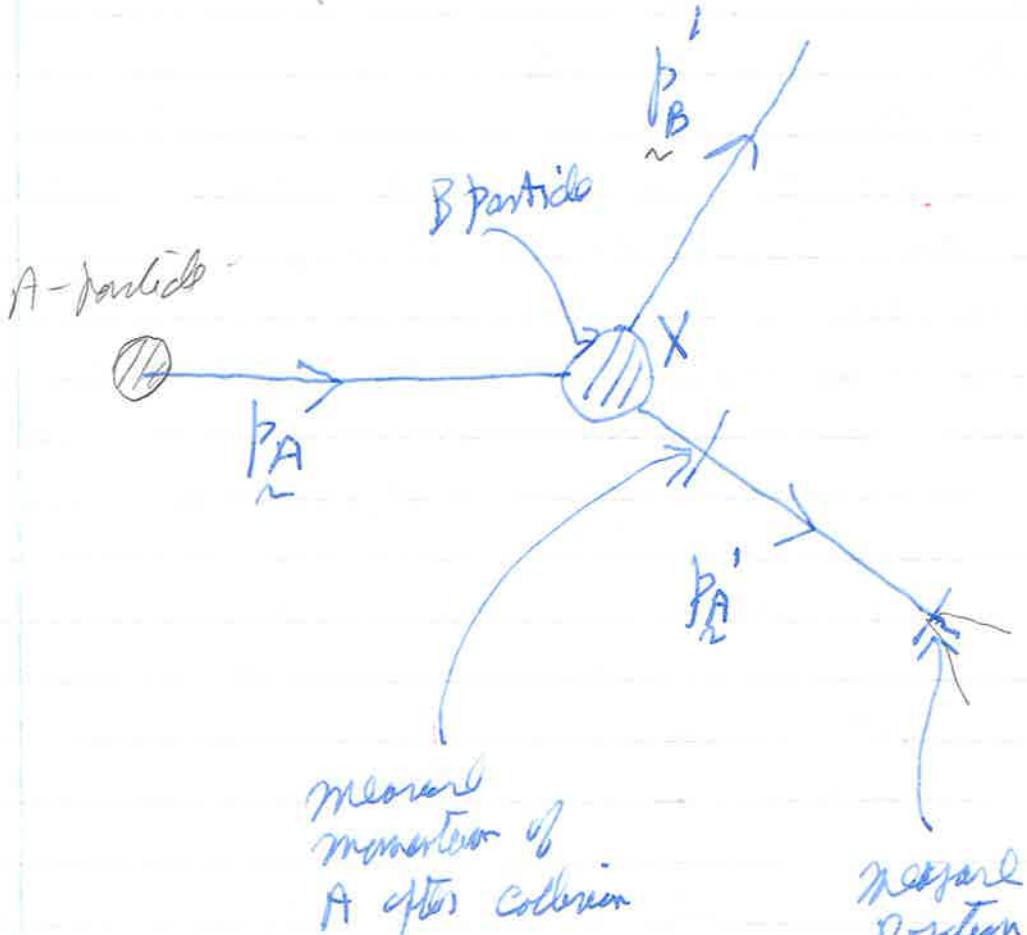


Figure 1 A schematic version of Popper's 1934 thought experiment

in matters of philosophy, the possibility that a gross mistake made by a nobody (like myself) may have had an influence on a man like Einstein never entered my head.

I shall now briefly describe the thought experiment, but with some complications that makes the evaluation of the experiment, in my belief, more transparent.

Popper's idea was to consider the scattering of two particles, call them A and B, where A has a sharp momentum and B a sharp position. (In Popper's actual experiment the collimator is between a parallel beam and a diverging beam. I am only proposing using the origin of divergence as the point of collimation — what Popper refers to as the Schnitt punkt. This greatly simplifies the geometry of the experiment.)

Referring to Fig. 1, A has a sharp momentum $\underset{\sim}{p}'_A$ and collides into a fixed momentum state $\underset{\sim}{p}_A$. B has initially a sharp position at the point X and recoils into a momentum superposition state $\underset{\sim}{p}'_B$. An unknown momentum $\underset{\sim}{p}_B$ is absorbed from the B particle, but this can be computed from conservation of momentum, i.e.

$$\underset{\sim}{p}_B = \underset{\sim}{p}'_A + \underset{\sim}{p}'_B - \underset{\sim}{p}_A \qquad (1)$$

⇒ Event Funnel.

Suppose now that we don't know the magnitude of B's final momentum but only its direction, i.e. we don't know $|\underset{\sim}{p}'_B|$. →

But this can be calculated from conservation of

energy, if we have measured $|p_A'|$ as well as the final direction of the scattered A particle. Popper now wants to show how to predict by measurements on the scattered A particle not only the recoiling momentum of the B particle but also its recoiling position at any given time. Since the recoil starts at X and we know the momentum and hence velocity of the recoiling particle, they as calculated from the measurement of p_A', we can predict the position of the recoiling particle (rounded up from the time at which the collision occurs). To find this, Popper, all we need to do is to measure the position of the scattered A particle after a given time after the momentum measurement, and retrodict from the former velocity of the A particle after the collision the time at which it must have emerged from X, i.e. the time of collision.

So putting all this together, by making momentum and position measurements on A, we can predict the momentum and position simultaneously for the recoiling B particle.

The flaw in Popper's argument is that measuring the momentum of the recoiling B particle necessarily affects the possibility of predicting its position at still earlier times. For example if we measure the momentum by the Doppler shift of very low frequency radiation, then an accurate measurement of the frequency requires a long wavetrain, i.e. a long duration of time for the irradiation, during which time the average

velocity of the B-th particle cannot be exactly specified. It is easy to show that this exactly prevents us from retrodicting the position of the B-th particle before the momentum measurement, and hence prevents us from inferring the locus at which the recoil particle emerges from X. An alternative proposal put forward by Popper was to measure the momentum by means of a selective filter. But this again would disturb the position of the recoil particle, for example a wavepacket of precise location incident on the filter would be inevitably 'spread out' by the action of the filter in selecting a particular narrow band of wavelengths from the wavepacket.

What EPR do, by contrast, is to devise an experiment in which by measuring either the momentum or position of one particle the corresponding momentum or position can be inferred for the other particle. But since both the measurements cannot be made simultaneously, we cannot predict simultaneous values for the momentum and position of the other particle. Had we been able to do this a conceptual selection of a 'super-pure' ensemble of the recoil particle would be possible, with no dispersion in momentum or position, but this would contradict the Heisenberg scattering relations, that Popper regards as the correct interpretation of Heisenberg's uncertainty principle. In LSD, ~~301~~ 245-246 and 301, Popper tries to argue that his thought experiment is not ruled out by violating

the objective scatter relations. But I find the discussion here quite unconvincing, confusing the selection of a sub-ensemble by conditionality on a random variable, with the controllable selection of a sub-ensemble by predicted selection. So without going into any details of the proposed experiment its purported conclusion actually contradicts a theorem of the formalism probing sub-pure states.

Popper returned to the matter of thought experiments in Appendix *XII of LSD entitled 'On the Use and Misuse of Imaginary Experiments, Especially in Quantum Theory'.

Popper warns against the ~~ubiquitous~~ use of imaginary experiments (Popper's italics) (LSD, 443). Great care must be taken not to introduce idealizations or other special assumptions unless they are favourable to an opponent, or such that any opponent would have to accept them (LSD, 444).

It is not clear that Popper heeded his own warnings in these matters as will become clear as we proceed to describe the next thought experiment that he devised in order to dispose the orthodox Copenhagen interpretation of quantum mechanics.

In 1982, in the new introduction to Volume 3 of the Postscript to the Logic of Scientific Discovery Popper describes what he ~~has elsewhere~~ terms an 'extension of the EPR argument' (~~LSD~~ QTSP 27 ff.).

The idea behind the experiment was to test whether knowledge alone is sufficient to create "uncertainty" and, with it scatter (as is entailed under the Copenhagen interpretation), or whether it is the physical situation that is responsible for the scatter.

Referring to Fig. 2., Popper proposes a source S from which pairs of particles are emitted in opposite directions in an EPR state, i.e. such that the momenta and the positions of the particles are correlated. The correlated particles are selected through slits A and B, which are sufficiently wide that there is no appreciable diffraction as they pass through the slits, and then fire off, in succession, Geiger counters. arranged, in a semicircle behind the slits, the counters firing between b_1 and b_2 behind the B slit and between a_1 and a_2 behind the A slit as indicated in the figure. For simplicity we just consider particles moving in the x–y plane of the diagram.

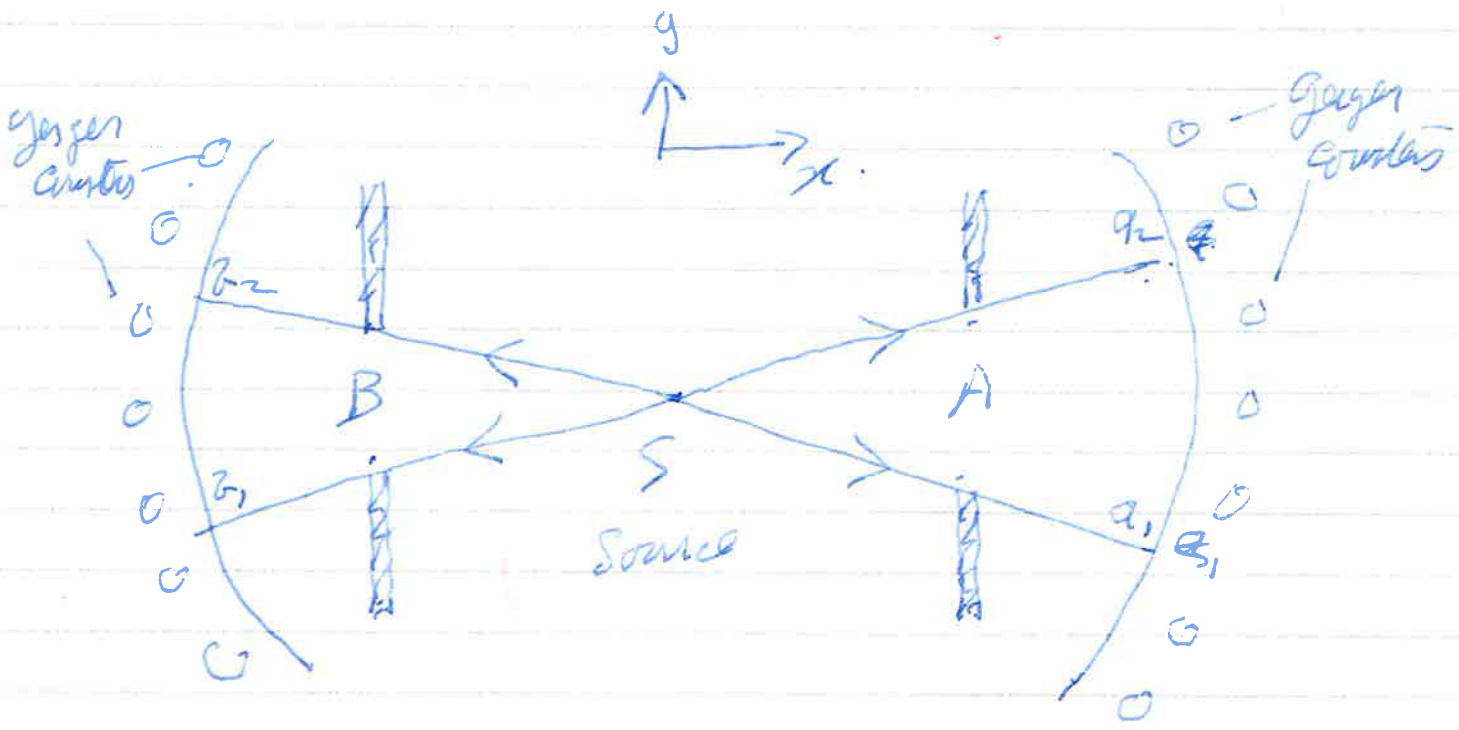


Figure 2 Popper's 1982 Thought Experiment

Since the momenta are correlated, b_1 goes with a_2, and b_2 with a_1, and so on. Now Popper proposes narrowing the A slit as illustrated in Fig. 3. Since the A slit is effectively restricting the y-coordinate of the particles passing through it and thus as a result of the Position Correlation, the y-coordinate of the particle passing through B is also more tightly confined as it ~~has~~ passes the A slit, and thus according to the Copenhagen interpretation the more accurate knowledge of the y-coordinate of the particle passing through the wide B slit would produce a greater in the transverse momentum, so, courses over the wider arc b_1 to b_2 will now fall (Of course there will be a corresponding scatter caused by narrow A slit).

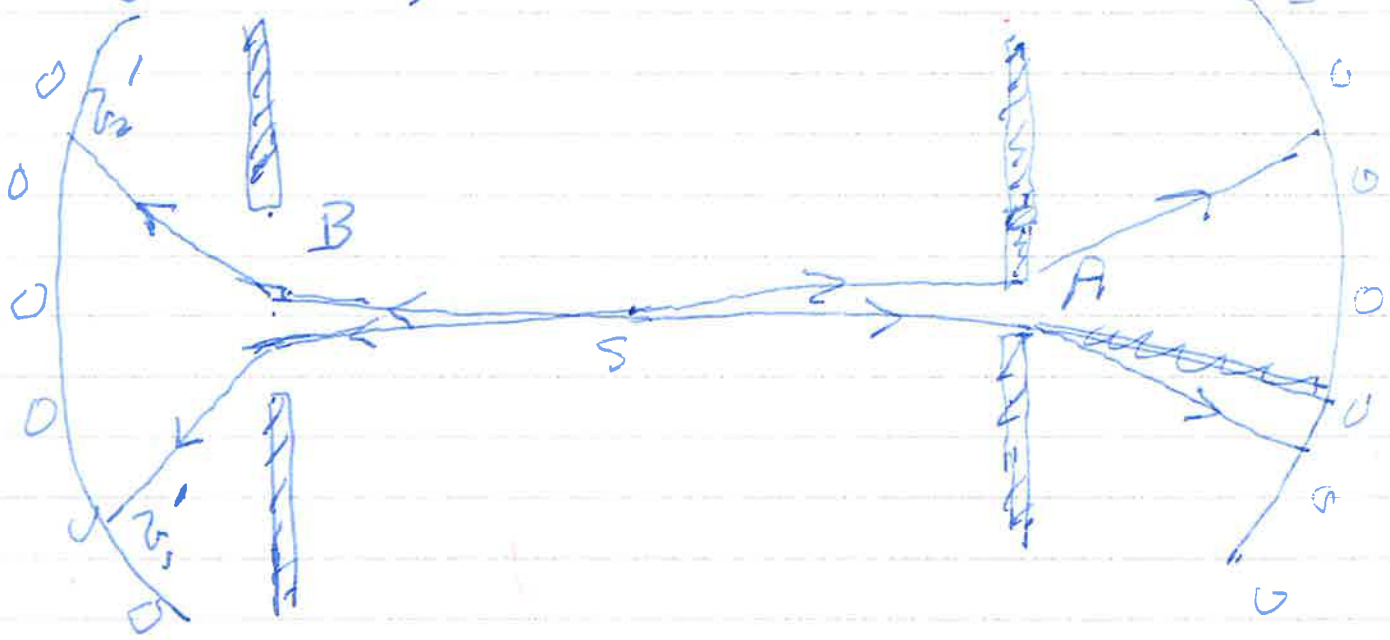


Figure 3 The Effect of narrowing the A slit according to Popper is to produce wide-angle scatter behind the wide slit B

Popper is convinced that this effect would not happen, so if performed the experiment would according to Popper, constitute a decisive refutation of the Copenhagen interpretation.

The flaw in Popper's argument [3] is that he misunderstands the nature of the EPR correlations.

The EPR state at the time $t=0$ of emission of the two particles, in respect of the transverse y-direction is of the form

$$|\Psi_0\rangle = \int_{-\infty}^{\infty} |y\rangle \otimes |y\rangle \, dy \qquad (2)$$

$$= \int_{-\infty}^{\infty} |p_y\rangle \otimes |-p_y\rangle \, dp_y \qquad (3)$$

The form (2) demonstrates the position correlation and the form (3) the momentum correlation.

So the EPR source, according to (2) is not a point source, like S in figs. 2 and 3, but an infinite incoherent line source. Why incoherent? Because for any observable A_1 of particle 1, for example, the expectation value at time t is

$$\langle \Psi_t | A_1 | \Psi_t \rangle = \int_{-\infty}^{\infty} \langle y_{1t} | A_1 | y_{1t} \rangle \, dy$$

where $|y_{1t}\rangle$ is the time-evolved state (4) at time t which starts at $t=0$ in an eigenstate $|y\rangle$ of position.

Similarly for observables referring to particle 2, the expectation values are additive — there is

interference between Schrödinger waves
occurring at different values of y.
So Popper's experiment with an EPR
source looks like Figs. 4 and 5 showing
wide angle ½ firing of the counters when
the A slit is wide, just the same as
when it is narrow, i.e. determining which
the A slit has no effect on which of
the counters behind the B slit fire. So
the 'Popper effect' is not predicted
according to the formalism of quantum
mechanics and left not predicted according
to any interpretation of that formalism,
in particular it is not predicted by
the Copenhagen interpretation.

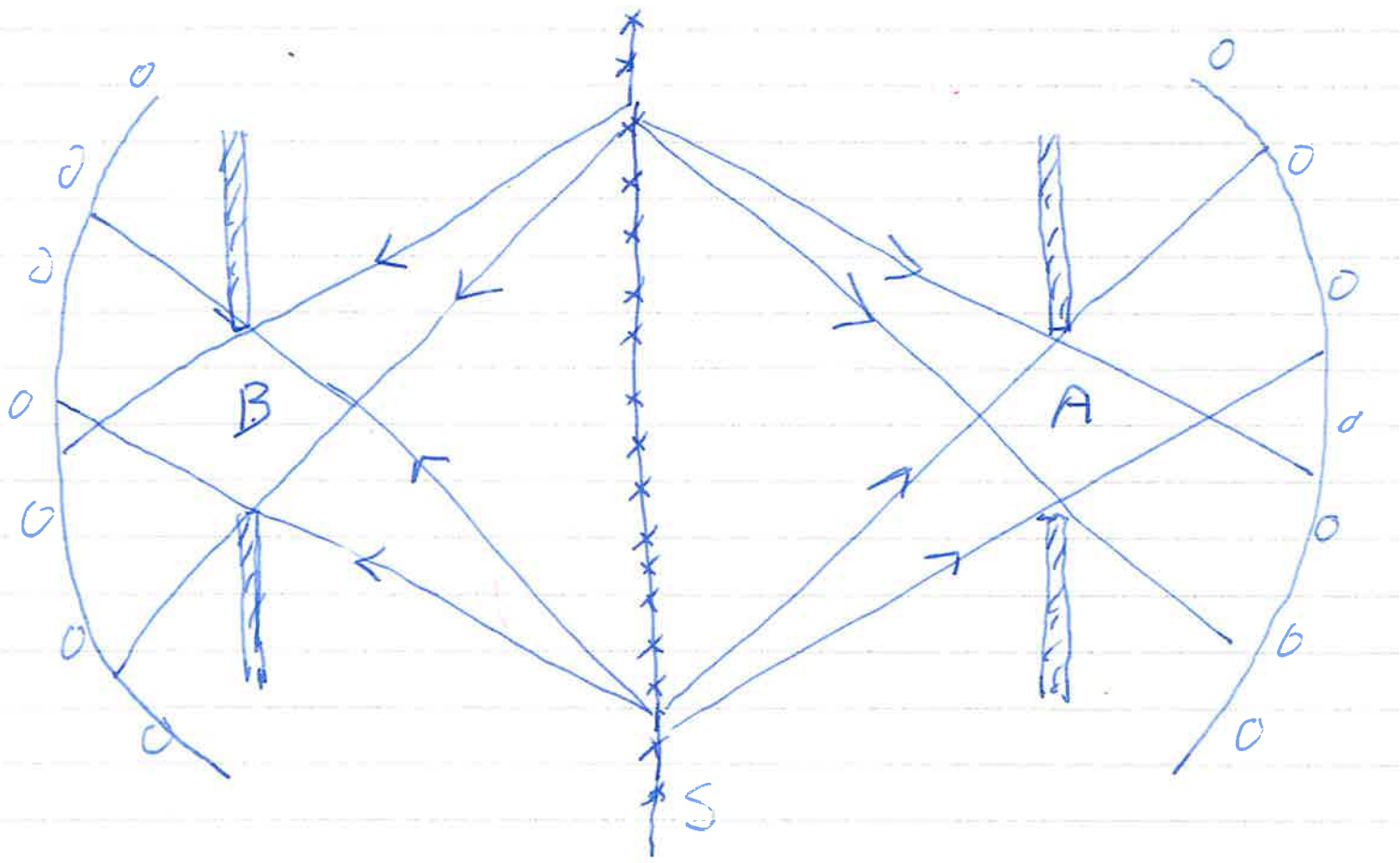


Figure 4 The EPR source with wide slits.
All counters fire on both sides of the experiment

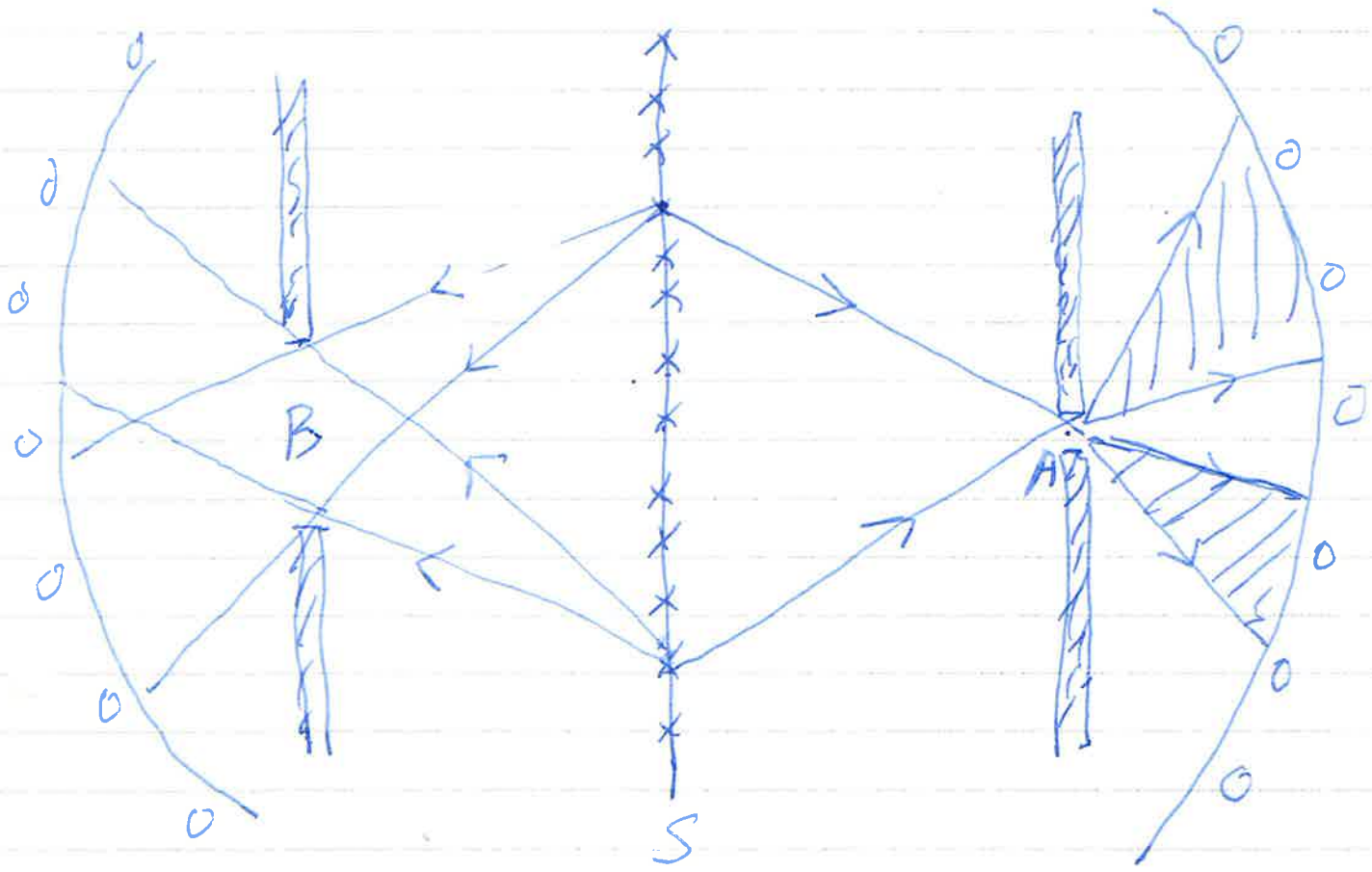


Figure 5 EPR source with a narrow slit at A. Notice diffracted effects behind A, but all counters fire on both sides of the apparatus.

When I showed this diagram to Popper, he refused to accept that I had a general argument that removing slit A could not make a counter fire behind B that would not have fired when A was wide. Perhaps by altering the geometry he could get what he wanted. To get rid of the wide-angle firing behind B on all encounters it is already necessary to truncate the low fringe. But truncating the EPR source by replacing the infinite limits in Eqn. (2) by finite limits,

then we lose the momentum conservation, i.e. we can no longer rewrite (2) in the form (3). In other words, using a truncated source, a narrow beam as the right in Fig. 3 does not constitute evidence against a narrow beam on the left, with resulting diffraction as Popper supposed. Fig. 3 should actually be replaced by Fig. 6 showing no actual diffraction between Edward B. as compared with the situation with both slits wide as illustrated in Fig. 2.

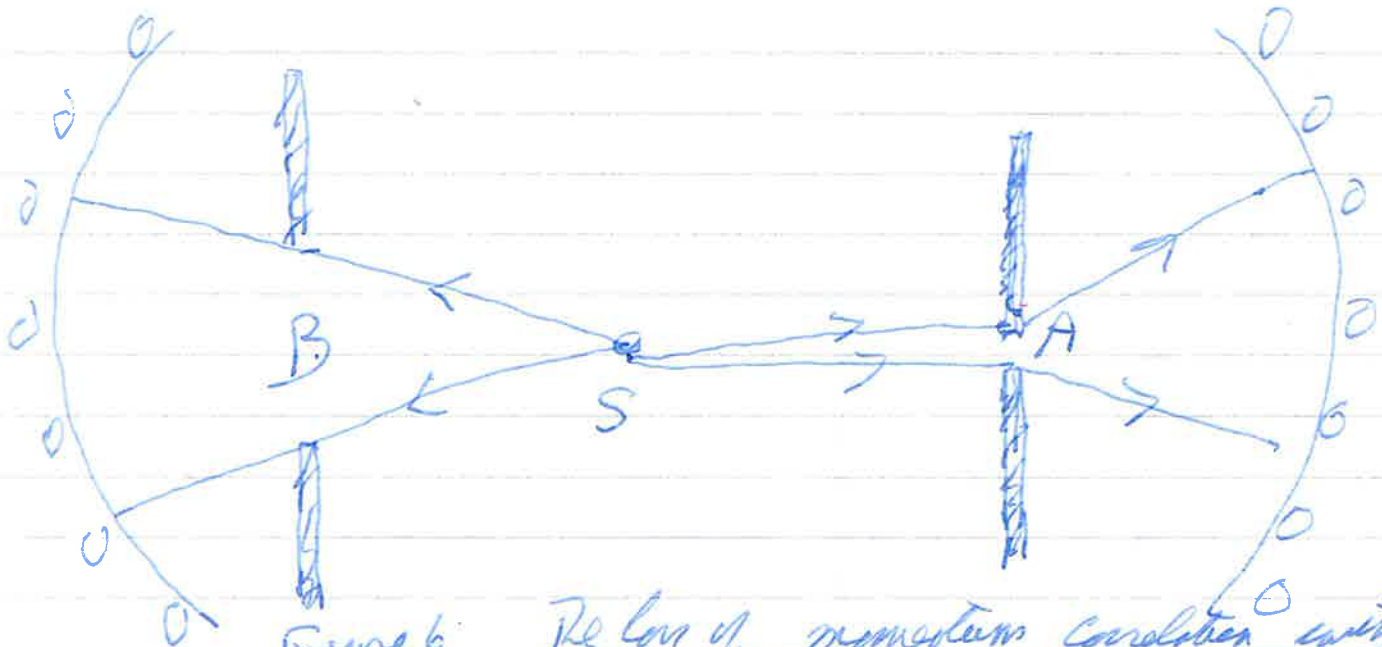


Figure 6. Loss of momentum correlation with a point source, localized slits

But Popper was still not convinced!
So I provided the following general proof.
Consider an observable A for the particle passing through the A slit with eigenvalues a_i, and similarly for B on the left with eigenvalues b_j.
Then the A and B channels are sorted, in an arbitrary state $|\psi\rangle$

Insertion Figure 7 on A-13

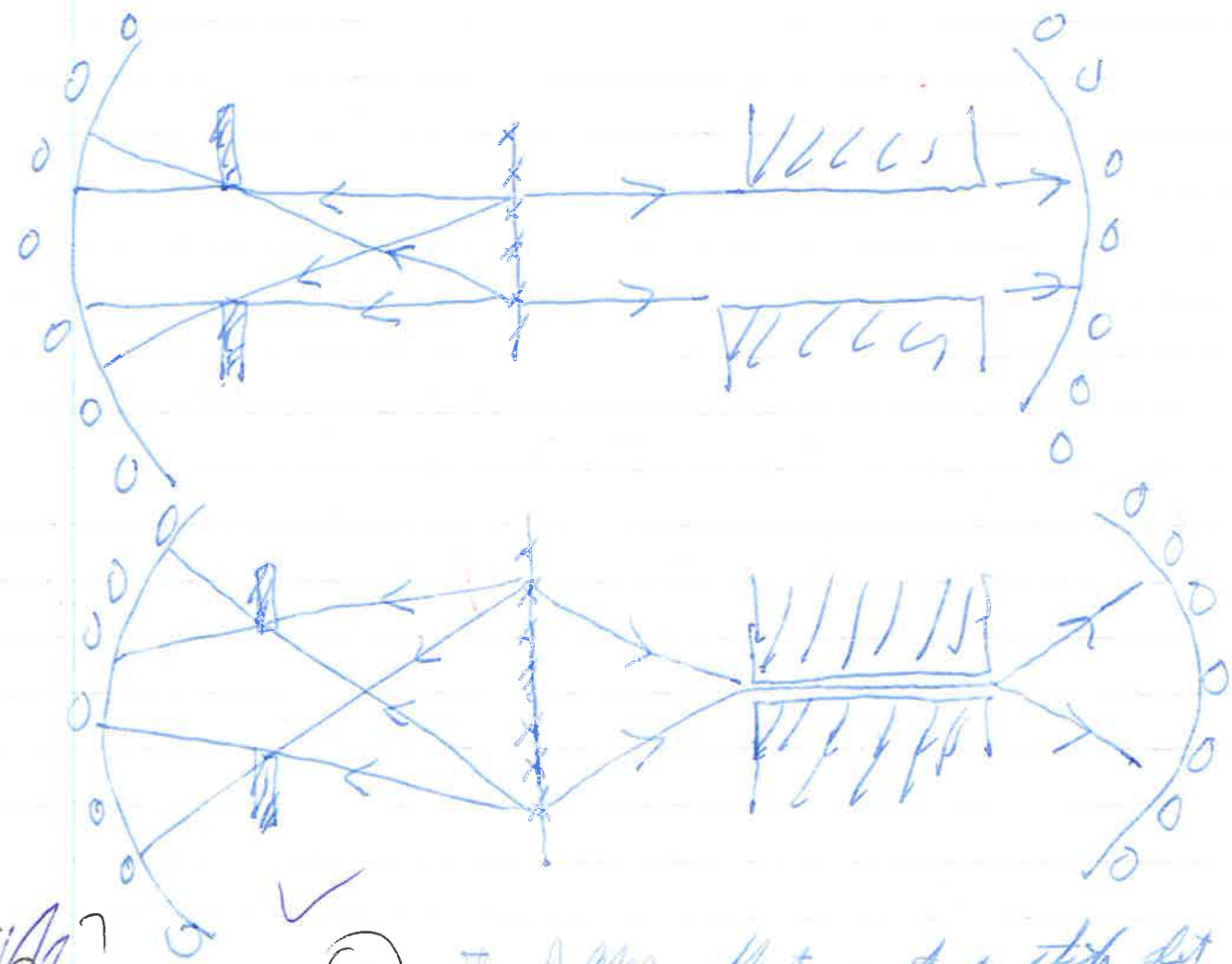
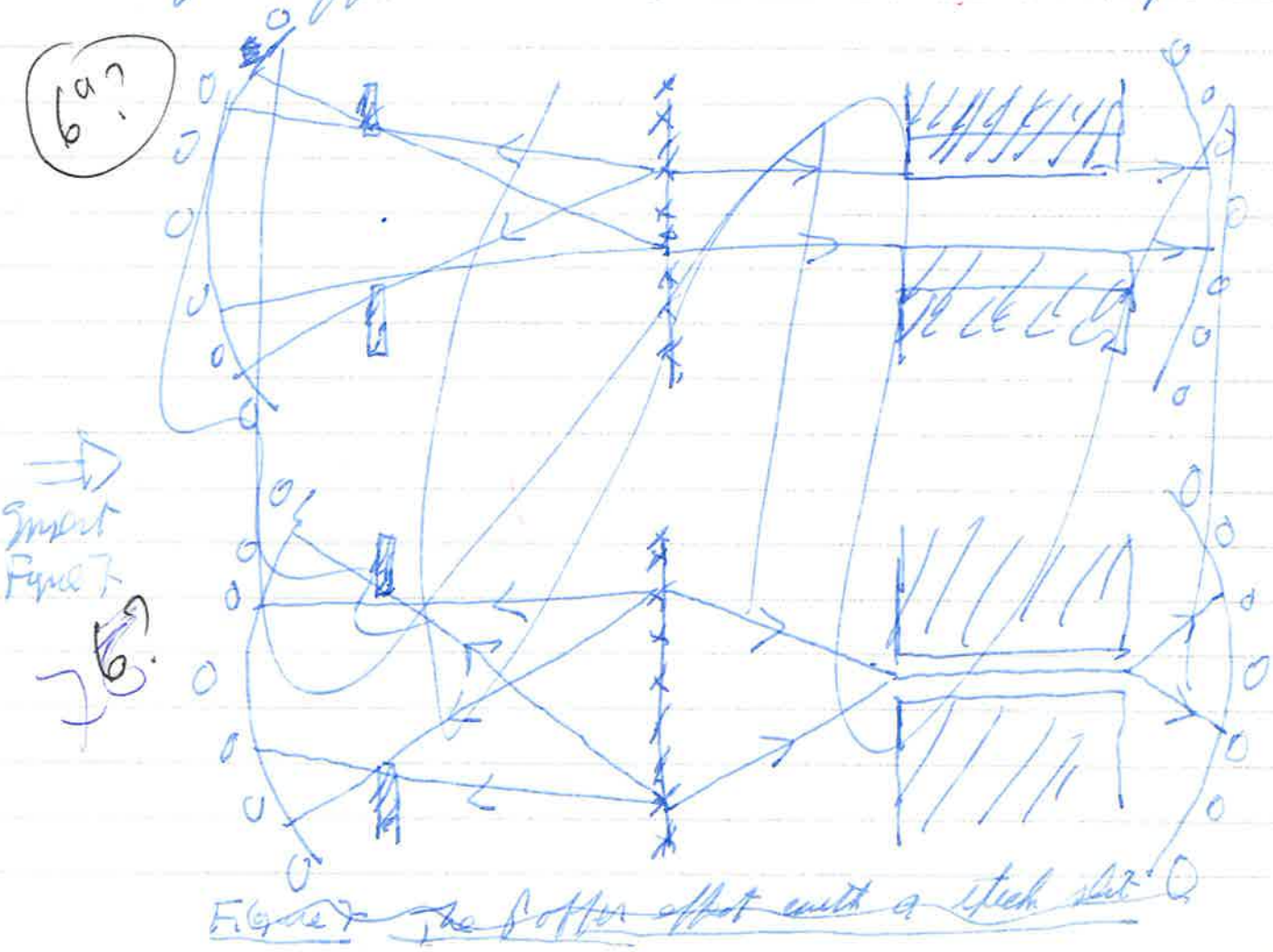


Figure 7 The Doppler effect and a thick slit

$$\text{Prob}^{\Psi}(b_j) = \sum_i \text{Prob}^{\Psi}(b_j/a_i) \times \text{Prob}^{\Psi}(a_i) \qquad (5)$$

Now suppose $\text{Prob}^{\Psi}(b_j=0)$ and $\text{Prob}^{\Psi}(a_i)\neq 0$ for some particular index i.
Then (5) implies that, under the condition $\text{Prob}^{\Psi}(b_j/a_i) = 0$, i.e. selecting a sub-ensemble on the left by conditionalizing on the right with an event that has a non-zero probability of occurring cannot convert a zero probability for b_j into a non-zero probability for b_j.

By a curious irony it is possible to produce the Copper effect, but not in the way Copper thought, by using a thick A slot.
The effect is illustrated in Fig. 7.



Insert Figure 7.

Figure 7. The Copper effect with a thick slit.

where we suffer the thickness of the A/ slit is very long compared with its width. The increased angle of fanning behind the A slit is now produced by the fact that due to diffraction effects at the narrow A slit we can actually localize, not a sub-ensemble, but a large ensemble of particles in the space as compared with the case of the wide A slit.

2.3 Indeterminism and Probabilities

Popper's approach to the quantum theory is based on two key ideas:

a) the prevalence of indeterminism in physics. Instead of the slogan 'all clouds are clocks', Popper wants to substitute 'all clocks are clouds' (OK, 215). His arguments for indeterminism apply in classical physics just as much as in quantum physics. They are based, for example, on views of capitalabilities that arise in classical mechanics or logical paradoxes produced by attempts at self-prediction, and the pervasive operation of what Popper calls the Oedipus-effect (OU, 66) whereby the very fact of making a prediction can influence the predicted event.

There are three elements in scientific determinism roughly speaking the possibility of a Laplacian demon being able to predict the future. But Popper also attacks what he calls metaphysical determinism, the view, picturesquely, that the future is 'coiled up',

in the present. For Popper this denies the reality of time and the possibility of real novelty arising in the Universe. Popper here strongly opposed Einstein who defended determinism ("God does not play dice ...") Popper's discussion of the conversation with Einstein as a freedom in 1950 he refers to Einstein as ~~the new Parmenides~~. Einstein – Parmenides (UQ, 130) Popper's real motivation for his detestation of determinism lay perhaps in his belief in human freedom, the unpredictability of a Mozart symphony or a Beethoven sonata, the development of new organs of species, the designs of his World 3, that created evolution is outside the powers of World 1 alone and that World 1 is crucially affected by World 3, via the mediation of World 2, and so on.

B) For that reason Popper thinks that probabilities in physics cannot, in principle, be objective. How could human ignorance produce genuine physical effects? Popper originally held a frequency view of probability but the predictions of stable statistic regularities (i.e. of random sequences) was for Popper a physical fact that needed explaining via an objective tendency, and this led him in the 1950's to 'his propensity interpretation'. This he expanded as particularly well suited to emphasize the creative elements which he took for granted in the uncertainty of uncertainty relations or quantum theory.

3.4. State Preparation and Measurement

Popper regarded the Heisenberg Uncertainty relations as limitations on the possibility of producing homogeneous ensembles with precise values of position x and momentum p, for example.
So Heisenberg had discovered a limitation on state preparation, not a limitation on measurement. When we measure x or p this is a backward looking experiment associated with the forward looking experiment of state preparation, and such measurements are necessary to test the ~~scatter~~ statistical scatter relations expressed in the Heisenberg ~~relations~~ principle.
Moreover, Popper says that he believes that between interactions particles behave classically, i.e. following Newtonian straight-line trajectories, but when interactions occur they get disturbed in an ~~ontologically~~ ontologically stochastic fashion and this is what produces the quantum-mechanical scatter.
As an analogy Popper often referred to what he calls the pin board (i.e. a form of bagatelle - cf., e.g., A, I, 5, p, 72, 87, 153). Here the balls roll deterministically between impacts with the pins. The statistical distribution of the balls at the bottom of the board is the manifestation of a propensity to produce ordered results, the final position of each individual rolling ball. The propensity is a property of the whole ~~set~~-up of pins and balls and is not to be thought of as a property of the individual balls themselves. This, for Popper, is the reason why what he calls

'the great quantum muddle' (QTSS, 52).
The mistake here is like treating the average height of people in a room as a property of each particular person in the room. My own view is that it is perfectly legitimate to regard the quantum-theoretical properties as properties of the particles, properties manifested in the context of particular entanglement arrangements. This means of course that there are as many properties as there are entanglement arrangements, so, talking Popper, it may sound extravagant to talk of 'the' property as belonging to the entangled ensemble but it does not seem to be mandatory to 'talk' in this way (~~as Redhead (1987, 249)~~).

Returning to Popper on the pin board, changing the arrangement of the pins changes the propensity – what the arrangement of the pins sets out here is a sort of landscape full of attractors and repellers. Popper sees the discovery, in a grand sort of way, the two-slit experiment. The closing of a slit is like removing a pin from the pin board. Even if the ball on a particular occasion never hits the pin nonetheless the propensity changes. Popper, of course, stresses (in response to a critique of Feyerabend[4]) that the pin board does not exhibit the characteristic interference phenomena of the two-slit experiment. To explain that is a matter for the physics of the relevant properties. Popper generally believes in the Lande afterward[5], that the effect of the two slits on the beam of electrons is related to

the paradoxicality of the structure, i.e. the separation of the slots which controls the transfer of momentum to the electron as it passes through one of the slits. If we close a slit the change in the sort of object that the electron is interacting with, and hence the character of the interaction.

Turning to another aspect of Penrose's (or Einstein's) collapse of the wave function, a projection postulate. this is often regarded as a quite unproblematic consequence of conditionalizing a probability distribution on the outcome of an experiment (STSP, 78). Consider a coin toss. When the coin lands heads, the probability of heads jumps from ½ to 1, and the collapse of the wave function is just an instance of this type of behaviour.

Let us look at this from the point of view of joint distributions. In standard probability theory one defines conditional probabilities in terms of joint distributions. Thus $Prob(A/B) =_{DF} Prob(A \& B) / Prob(B)$, provided $Prob(B) \neq 0$. Popper's own approach to probability theory starts with conditional probabilities as basic and proceeds to joint distributions employing the defining ~~$Prob(A \& B) =_{DF} Prob(A/B) \cdot Prob(B)$~~

$Prob(A \& B / C) =_{DF} Prob(A / B \& C) \cdot Prob(B/C)$ (cp. LSD, 332).

But either way of proceeding assumes commitment to joint distributions such as $Prob(x \& p)$ (perhaps conditionalized on an experimental set-up) for incompatible observables such as x and p. So what is the status of joint distributions and simultaneous

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Measurability in quantum mechanics.?

Suppose we measure an observable Q and find the value q, so the new state (according to the projection postulate) is the eigenket $|q\rangle$.

If now we measure an incompatible observable Q' and find the value q', then it seems reasonable to claim that for the state $|q\rangle$ Q has the value q and Q' the value q'.

Of course we cannot use this knowledge to predict the value of Q' after we measured Q'. This might well differ from q due to the disturbing effect of the measurement of Q'.

But can we assign Q and Q' when the state $|\psi\rangle$ is not an eigenstate of Q (or Q')?

A typical proposal here is to measure an observable, call it U which is compatible with Q and has the same numerical eigenvalues as Q', and in the state $|\psi\rangle$, has the same probability distribution as Q'. So Q and Q' are matched probabilistically, but it does not follow that on a particular occasion the result for U is the same as the result we would have found if we had measured Q'.

The classic example of this is the time-of-flight measurement of momentum. (We consider a one-dimensional model.) An indirect measurement of position locates a particle sharply at the origin at time $t = 0$, then if we measure the position X again at a later time t, the quantity $U = \frac{m \cdot X}{t}$ is distributed probabilistically in the same way as the momentum scattered by the earlier position measurement. But measuring X allows us to assign the value of U, so the combination of values x for X and u for U (where $u = \frac{mx}{t}$) constitutes a

joint measurement of position and momentum for the particle. The question is, does the U measurement give the same result, on a particular occasion as a 'direct' measurement of momentum e.g. by bending in a magnetic field, or using the Doppler shift to measure the velocity, and hence the momentum. Note that for all these direct measurements, anyway they are of the so-called first kind in that the projection postulate applies, the results of the procedure can be checked by applying the other procedures, since they are also compatible procedures. But in the case of the time-of-flight approach, after the X measurement the particle is destroyed, so the value before the X measurement cannot be checked by a subsequent direct measurement.

Were this the case, if one knows the form of the particle after its initial position measurement at $t = 0$ as $\psi(x)$, then U must be the unique momentum that links the initial and final position measurements, although as we have seen this is something that cannot be checked or tested.

Nonetheless all this tells us about the joint distribution for x and p. Namely it is of the form $\pm(p - m\frac{x}{t})$. $\text{Prob}(x)$, which contains the joint density we want. The right marginals for x and p work for a particular state. Indeed joint distributions can always be defined for particular states e.g. take the joint density to be of the form $\text{Prob}(p) \times \text{Prob}(x)$. Again this contains the right marginals. But if we ask the

quotes is there a quantum-mechanical observable that measures the joint quantity 'x and p' and returns the right marginals in all states the answer is 'NO', exactly to an important theorem of Fine (~~1973~~).
Constructions in the literature[7] (~~Ref, Ref - Wigner (1932)~~) that do return the right marginals in all states, do not give non-negative values for the joint distribution and so these do not qualify as bona fide probabilities.
So it is difficult to fit joint distributions ~~into the form~~ for incompatible observables into the formalism of quantum mechanics and indeed Abner Fine ~~&~~ has urged that we should regard them as a phase-space reconstruction of quantum mechanics. As Fine says joint distributions in probability theory (p) arise as general when x and p, for example, are regarded as random variables (as in ordinary probability theory) and we don't have to make this overly strong assumption[8] (~~see Fine 1982~~).
It would be very interesting to know Wigner's views on this question. As far as I know he never refuted Fine's arguments on this point.

4. Nonlocality and Bell's Inequality

Another important work in the foundations of quantum mechanics, on the level of realist construal espoused by Popper, is the question of proofs of nonlocality and the theorems predicted on experimental verified violation of the famous Bell inequality.

Popper made two sorts of comment here. Firstly, if the experiments and their interpretations were taken at face value, then he regarded the Aspect experiment for example, as a crucial test of the Lorentz versus the Einstein interpretation of the relativity transformation equations. Unfortunately other crucial experiments have cast doubt on the Lorentz preferred reference frame, an earlier hope of good friends.

But secondly, Popper drew attention to the mere fact that the theoretical proofs of the impossibility of local hidden-variable theories for experiments such as Aspect's, might contain technical flaws. He gave support to the work of Thomas Angelides[9] who sought to demonstrate local models of these experiments. Roy Lee Weinstock, who corresponded with Popper, just before his death, was pressing the validity of this work. In my view the models were not correctly described as local. Popper himself admitted that the whole matter was too technical for him to fully check everything, but urged that the latest work of Angelides should be fully applied to the literature. This is something I propose to do on a future occasion.

At first sight it might appear that, with

* Grafton
Indeed, he was critical of Boston's
Judge - harsh approach to the
just reason became of Boston's commitment
to determine

Popper's confusion in understanding the shareholder-value approval[10] (see, e.g., Ostlund (1989), 98 ff.) is due to his inconsistent and his other views. First he commences to determine behaviour between spheres coupled with his advance to a theory of portfolio measurement, means that the measurement outcomes are deterministically related to the state of the particles after they have left the source. Hence the determinable hidden-variable proofs of the Bell inequality are the ones about to that need to be examined by Popper, consistently used as means he opposed in other contexts.

5. Conclusion

Popper showed (QTSP, 6) that the strongest reason for my own opposition to the Copenhagen interpretation lies in its claim to finality and completeness. I entirely agree with the view that we should not take our criticism by fiat or authority. Popper fought a long battle against the Copenhagen interpretation at a time when anyone attempting to criticize orthodoxy was liable to be labelled at best as 'odd' or at worst a crank. But Popper's earlier arguments and criticisms were the product of a number of ordinary and reflected physicists. He has done a great deal to dispel this fiction by emphasizing the destructive values that interpretation and movement and trying to set up a clearer understanding of the true significance of the Copenhagen principle. I think above all by ~~pressing~~ pressing the attention to the dogmatic & unqualified character of the Copenhagenists. Because some detailed arguments are flawed this does not mean that the overall criticism has not been abundantly beneficial

Notes (to be inserted in the text at the relevant place)

1. In this paper Popper claimed to explain some ambiguity in the Birkhoff & von Neumann proof concerning the distinction between complement and orthocomplement on a lattice, and by using a plausible means - thereby suggesting concerning their lattice showed that it was actually distributive rather than non-distributive. For a detailed critique of Popper's argument, reference may be made to I. Schaible, 'Popper and Quantum Logic', The British Journal for the Philosophy of Science 25 (1974) 319-328.

2. For historical details see M. Jammer, The Philosophy of Quantum Mechanics (Wiley, New York, 1974), p. 178.

3. There are other critiques of the argument in the literature nothing broadly secular points to my ear. See, for example A. Sudbury, 'Popper's Argument of the EPR Experiment does not Test the Copenhagen Interpretation', Philosophy of Science 53 (1985) 470-476. and H. Krips, 'Popper, Propensities, and Quantum Theory', The British Journal for the Philosophy of Science 35 (1984) 253-282.

4. P. Feyerabend, 'On a Recent Critique of Complementarity', Philosophy of Science 35 (1968) 309-331; 36 (1969) 82-105.

5. A. Landé, Quantum Mechanics (Pitman, London, 1951)

6. A. Fine 'Probability and the Interpretation of Quantum Mechanics', The British Journal for the Philosophy of Science 24 (1973) 1-37.

7. See for example E. Wigner 'On the Quantum Correction for Thermodynamic Equilibrium', Physical Review 40 (1932) 749-759.

8 See A. Fine 'Logic, Probability, and Quantum Theory', Philosophy of Science 35 (1968) 101-111.

9. I. Stapleton 'Bell's Theorem: Does the Closure Hole Jeopardize Hopes for all Local Theories?' Physical Review Letters 51 (1983) 1819-1822. and 'On the Problem of a Local Extension of the Quantum Formalism', Journal of Mathematical Physics 34 (1993) 1635-1653. The first paper has been criticised by a number of people.

The second paper has not so far attracted critical comment in the literature.

10 See, for example M.L.G. Redhead, Incompleteness, Nonlocality, and Realism (Clarendon Press, Oxford, 1987), p. 98 ff.